PP-DSE MATH CP PAPER 2

HONG KONG EXAMINATIONS AND ASSESSMENT AUTHORITY
HONG KONG DIPLOMA OF SECONDARY EDUCATION EXAMINATION

## PRACTICE PAPER MATHEMATICS Compulsory Part PAPER 2

(11/4 hours)

## INSTRUCTIONS

- Read carefully the instructions on the Answer Sheet. After the announcement of the start of the examination, you should first stick a barcode label and insert the information required in the spaces provided. No extra time will be given for sticking on the barcode label after the "Time is up" announcement.
- When told to open this book, you should check that all the questions are there. Look for the words 'END OF PAPER' after the last question.
- 3. All questions carry equal marks.
- 4. ANSWER ALL QUESTIONS. You are advised to use an HB pencil to mark all the answers on the Answer Sheet, so that wrong marks can be completely erased with a clean rubber. You must mark the answers clearly; otherwise you will lose marks if the answers cannot be captured.
- You should mark only ONE answer for each question. If you mark more than one answer, you will receive NO MARKS for that question.

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6. No marks will be deducted for wrong answers.

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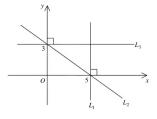
There are 30 questions in Section A and 15 questions in Section B. The diagrams in this paper are not necessarily drawn to scale.

Choose the best answer for each question.

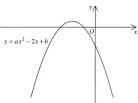
## Section A

- 1.  $x^3(2x+x) =$ 
  - A. 3x4.
  - B.  $2x^5$ .
  - C.  $3x^5$ .
  - D.  $2x^6$ .
- 2. If 3a+1=3(b-2), then b=
  - A. a+1.
    - B. a+3.
    - C.  $a + \frac{7}{3}$ .
    - D.  $a \frac{5}{3}$ .
- 3.  $p^2 q^2 p q =$ 
  - A. (p+q)(p-q-1).
  - B. (p+q)(p+q-1).
  - C. (p-q)(p-q+1).
  - D. (p-q)(p+q-1).

- 4. Let m and n be constants. If  $m(x-3)^2 + n(x+1)^2 \equiv x^2 38x + 41$ , then m =
  - A. -4 .
  - B. -1.
  - C. 3.
  - D. 5.
- 5. Let  $f(x) = x^4 x^3 + x^2 x + 1$ . When f(x) is divided by x + 2, the remainder is
  - A. -2 .
  - B. 0.
  - C. 11.
  - D. 31.
- 6. Let k be a constant. If the quadratic equation  $3x^2 + 2kx k = 0$  has equal roots, then k =
  - A. -3.
  - В. 3.
  - C. -3 or 0.
  - D. 0 or 3.
- In the figure, the x-intercepts of the straight lines L<sub>1</sub> and L<sub>2</sub> are 5 while the y-intercepts of the straight lines L<sub>2</sub> and L<sub>3</sub> are 3. Which of the following are true?
  - I. The equation of  $L_1$  is x = 5.
  - II. The slope of  $L_2$  is  $\frac{3}{5}$ .
  - III. The point (2,3) lies on  $L_3$ .
    - A. I and II only
    - B. I and III only
    - C. II and III only
    - D. I, II and III



- 8. The figure shows the graph of  $y = ax^2 2x + b$ , where a and b are constants. Which of the following is/are true?
  - I. a > 0
  - II. b < 0
  - III. ab < 1
    - A. I only
    - B. II only
    - C. I and III only
    - D. II and III only



- 9. The solution of 4x > x-3 or 3-x < x+7 is
  - A. x > -2.

  - B. x < -2.
  - C. x > -1.
  - D. x < -2 or x > -1.
- 10. John buys a vase for \$1600. He then sells the vase to Susan at a profit of 20%. At what price should Susan sell the vase in order to have a profit of 20%?
  - A. \$ 2.240
  - B. \$2304
  - C. \$2400
  - D. \$ 2500
- 11. If the circumference of a circle is increased by 40%, then the area of the circle is increased by
  - A. 18%.
  - B. 20%.
  - C. 40%.
  - D. 96%.

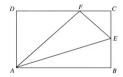
- 12. Let  $\alpha$  and  $\beta$  be non-zero constants. If  $(\alpha + \beta): (3\alpha \beta) = 7:3$ , then  $\alpha: \beta =$ 
  - A. 5:9.
  - B. 9:5.
  - C. 19:29.
  - D. 29:19.
- 13. If z varies directly as x and inversely as  $y^2$ , which of the following must be constant?
  - A.  $\frac{x}{v^2z}$
  - B.  $\frac{z}{rv^2}$
  - C.  $\frac{yz}{r^2}$
  - D.  $\frac{xz}{v^2}$
- 14. 0.009049999 =
  - A. 0.00905 (correct to 3 decimal places).
  - B. 0.00905 (correct to 3 significant figures).
  - C. 0.00905 (correct to 6 decimal places).
  - D. 0.00905 (correct to 6 significant figures).
- 15. In the figure, O is the centre of the sector OABC. If the area of  $\Delta OAC$  is  $12~{\rm cm}^2$ , find the area of the segment ABC.
  - A.  $3(\pi 2) \text{ cm}^2$
  - B.  $3(\pi 1) \text{ cm}^2$
  - C.  $6(\pi 2) \text{ cm}^2$
  - D.  $6(\pi 1) \text{ cm}^2$



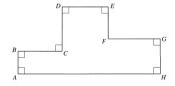
- 16. The figure shows a right circular cone of height 8 cm and slant height 17 cm. Find the volume of the circular cone.
  - A.  $255\pi \text{ cm}^3$
  - B.  $345\pi \text{ cm}^3$
  - C. 480π cm<sup>3</sup>
  - D.  $600\pi \text{ cm}^3$



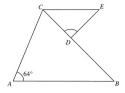
- 17. In the figure, ABCD is a rectangle. E is the mid-point of BC. F is a point lying on CD such that DF = 2CF. If the area of  $\Delta CEF$  is  $1 \text{ cm}^2$ , then the area of  $\Delta AEF$  is
  - A. 2 cm<sup>2</sup>.
  - B.  $3 \text{ cm}^2$ .
  - C. 4 cm<sup>2</sup>.
  - D.  $6 \text{ cm}^2$ .



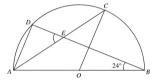
- 18. In the figure, AB = 4 cm, BC = CD = DE = 8 cm and FG = 9 cm. Find the perimeter of  $\triangle AEH$ .
  - A. 60 cm
  - B. 74 cm
  - C. 150 cm
  - D. 164 cm



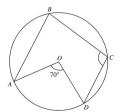
- 19. In the figure, AB = BC and D is a point lying on BC such that CD = DE. If AB // CE, find  $\angle CDE$ .
  - A. 52°
  - B. 58°
  - C. 64°
  - D. 76°



- 20. In the figure, O is the centre of the semi-circle ABCD. AC and BD intersect at E. If AD//OC, then  $\angle AED =$ 
  - A. 48°.
  - B. 55°.
  - C. 57°.
  - D. 66°.



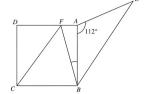
- 21. In the figure, O is the centre of the circle ABCD. If  $\widehat{AB} = \widehat{BC} = 2\widehat{CD}$ , then  $\angle BCD =$ 
  - A. 64°.
  - B. 87°.
  - C. 93°.
  - D. 116°.



22. In the figure, ABCD is a square. F is a point lying on AD such that CF//BE. If AB = AE, find ∠ABF correct to the nearest degree.



- B. 18°
- C. 22°
- D. 26°



23. For  $0^{\circ} \le \theta \le 90^{\circ}$ , the least value of  $\frac{30}{3\sin^2 \theta + 2\sin^2(90^{\circ} - \theta)}$ 

- В. 6.
- 10.
- D. 15.

Which of the following parallelograms have rotational symmetry and reflectional symmetry?



II. 6





III.

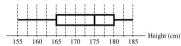
- A. I and II only
- B. I and III only
- C. II and III only
- I, II and III D.

- 25. If the point (-2,-1) is reflected with respect to the straight line y=-5, then the coordinates of its image are
  - A. (-8,-1).
  - B. (-2, -9).
  - C. (-2,11).
  - D. (12,-1).

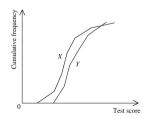
- 26. The coordinates of the points A and B are (1, -3) and (-5, 7) respectively. If P is a point lying on the straight line y = x + 2 such that AP = PB, then the coordinates of P are
  - A. (-2,0).
  - B. (-2, 2).
  - C. (0,2).
  - D. (3,5).

- 27. The equation of a circle is  $2x^2 + 2y^2 + 8x 12y + 3 = 0$ . Which of the following are true?
  - I. The coordinates of the centre of the circle are (-2,3).
  - II. The radius of the circle is 7.
  - III. The point (2,3) lies outside the circle.
    - A. I and II only
    - B. I and III only
    - C. II and III only
    - D. I. II and III

- 28. Two numbers are randomly drawn at the same time from four cards numbered 2, 3, 5 and 7 respectively. Find the probability that the sum of the numbers drawn is a multiple of 4.
  - A.  $\frac{1}{3}$
  - B.  $\frac{1}{4}$
  - C.  $\frac{1}{6}$
  - D.  $\frac{5}{16}$
- 29. The box-and-whisker diagram below shows the distribution of the heights (in cm) of some students. Which of the following is/are true?

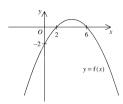


- I. The height of the tallest student is 180 cm.
- II. The inter-quartile range of the distribution is 15 cm.
- III. Less than half of the students are taller than 170 cm.
  - A. I only
  - B. II only
  - C. I and III only
  - D. II and III only
- 30. The figure below shows the cumulative frequency polygons of the test score distributions X and Y. Let m<sub>1</sub>, r<sub>1</sub> and s<sub>1</sub> be the median, the range and the standard deviation of X respectively while m<sub>2</sub>, r<sub>2</sub> and s<sub>2</sub> be the median, the range and the standard deviation of Y respectively. Which of the following are true?
  - ${\rm I.} \qquad m_1 > m_2$
  - II.  $r_1 > r_2$
  - III.  $s_1 > s_2$ 
    - A. I and II only
    - B. I and III only
    - C. II and III only
    - D. I , II and III



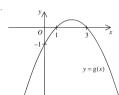
## Section B

31.

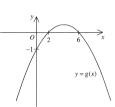


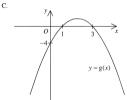
The figure above shows the graph of y = f(x). If 2f(x) = g(x), which of the following may represent the graph of y = g(x)?

A.

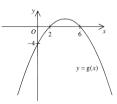


B.





D.



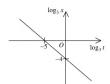
- B0000000023<sub>16</sub> = 32.
  - $11 \times 16^{10} + 23$ . A.
  - В.  $11 \times 16^{10} + 35$ .
  - $12 \times 16^{11} + 23$ . C.
  - $12 \times 16^{11} + 35$ . D.

- 33. If the roots of the quadratic equation  $x^2 kx + 3 = 0$  are  $\alpha$  and  $\beta$ , then  $\alpha^3 + \beta^3 =$ 
  - A.  $k^3$ .
  - B.  $k^3 3k$ .
  - C.  $k^3 9k$ .
  - D.  $k^3 12k$ .
- 34. If x is a real number, then the real part of (x+3i)(3+i) is
  - A. 3x.
  - B. x+3.
  - C. 3x + 3.
  - D. 3x-3.
- 35. The nth term of a sequence is 2n+3. If the sum of the first m terms of the sequence is less than 3000, then the greatest value of m is
  - A. 52.
  - B. 53.
  - C. 56.
  - D. 57.
- 36. Let b > 1. If  $a = \log_{12} b$ , then  $\frac{1}{a} =$ 
  - A.  $\log_b \frac{1}{12}$ .
  - B. log<sub>b</sub> 12.
  - C.  $\log_{12} \frac{1}{b}$ .
  - $D. \qquad \frac{1}{\log_b 12} \ .$

37. The graph in the figure shows the linear relation between  $\log_3 t$  and  $\log_3 x$ . If  $x = kt^a$ , then k =



- B. 81 .
- C.  $\frac{-4}{5}$
- D.  $\frac{-5}{4}$



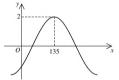
38. Let a be a constant and  $-90^{\circ} < \theta < 90^{\circ}$ . If the figure shows the graph of  $y = a \sin(x^{\circ} + \theta)$ , then

A. 
$$a = -2$$
 and  $\theta = -45^{\circ}$ .

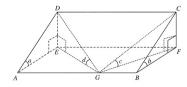
B. 
$$a = -2$$
 and  $\theta = 45^{\circ}$ .

C. 
$$a=2$$
 and  $\theta=-45^{\circ}$ .

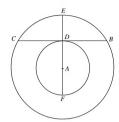
D. 
$$a=2$$
 and  $\theta=45^{\circ}$ .



- 39. The figure shows a right prism ABCDEF with a right-angled triangle as the cross-section. A, B, E and F lie on the horizontal ground. G is a point lying on AB such that AG: GB = 5:3. If ∠DAE = a, ∠CBF = b, ∠CGF = c and ∠DGE = d, which of the following is true?
  - A. a > c > d
  - B. a > d > c
  - C. c > b > d
  - D. c > d > b



- 40. In the figure, A is the common centre of the two circles, BC is a chord of the larger circle and touches the smaller circle at D. AD produced meets the larger circle at E. F is a point lying on the smaller circle such that E, D, A and F are collinear. If BC = 24 cm and DE = 8 cm, then EF =
  - A. 13 cm.
  - B. 16 cm.
  - C. 18 cm.
  - D. 20 cm.



- 41. If the straight line x-y=0 and the circle  $x^2+y^2+6x+ky-k=0$  do not intersect with each other, find the range of values of k.
  - A. 2 < k < 18
  - B. -18 < k < -2
  - C. k < 2 or k > 18
  - D. k < -18 or k > -2

- 42. Let O be the origin. If the coordinates of the points A and B are (18, -24) and (18, 24) respectively, then the x-coordinate of the orthocentre of  $\triangle OAB$  is
  - A. -14 .
  - B. 10.
  - C. 12.
  - D. 25.

- 43. Mary, Tom and 8 other students participate in a solo singing contest. If each participant performs once only and the order of performance is randomly arranged, find the probability that Mary performs just after Tom.
  - A.  $\frac{1}{2}$
  - B.  $\frac{1}{10}$
  - C.  $\frac{1}{4}$
  - D.  $\frac{1}{90}$
- 44. The mean, the variance and the inter-quartile range of a set of numbers are 40, 9 and 18 respectively. If 5 is added to each number of the set and each resulting number is then tripled to form a new set of numbers, find the mean, the variance and the inter-quartile range of the new set of numbers.

	Mean	Variance	Inter-quartile range
A.	120	27	69
B.	120	81	69
C.	135	27	54
D.	135	81	54

- 45. Let A be a group of numbers  $\{\alpha,\beta,\gamma,\delta\}$  and B be another group of numbers  $\{\alpha+2,\beta+2,\mu+2,\gamma+2,\delta+2\}$ , where  $\alpha<\beta<\mu<\gamma<\delta$ . Which of the following must be true?
  - I. The median of A is smaller than that of B.
  - II. The range of A and the range of B are the same.
  - III. The standard deviation of A is greater than that of B.
    - A. I and II only
    - B. I and III only
    - C. II and III only
    - D. I, II and III

END OF PAPER